

Content Clusters - Stage 3

Scope and sequencing by conceptual understanding

This is the scope... you create the sequence.

In this resource I provide possible ways of how groups of outcomes and their key ideas can be sequenced together based on the concepts they address. These are just examples and is not an exhaustive list of the clusters you can use to make connections across mathematics. I have used



the syllabus outcomes, sub strands and the mathematics key ideas document. When teaching for conceptual understanding (not just the knowledge of each sub strand) we need to make clear how the pieces of the mathematical puzzle fit together. To do this, our planning needs to reflect this belief - that mathematics is a complex web of interrelated ideas. For ideas on what these links are, see my Linkages across the syllabus document on the resources section of our website.

The scope of what we teach is described in the syllabus (this is the constant), the sequence of what and how we teach mathematics is a decision for individual teachers (this is the variable). These clusters can be used to create meaningful sequences of learning that focus on concepts and programs that still address common sub strands (across grades or classes) but allow for individual teachers to add additional key ideas or focus on specific aspects of the cluster that students either have misconceptions around or are developing conceptual understanding in. The clusters are numbered but are not written in teaching order. These clusters may be added to or updated in the future and newer versions will be released.

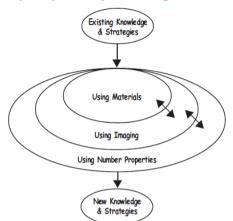


These clusters highlight the concept or main idea that ties each group of outcomes together, assisting teachers in making sense and meaning of the mathematics to students. When we think about the concepts or understandings first, we can think about what misconceptions students may have or what aspects of that concept they need next to connect their prior knowledge (the known) to create new knowledge (the unknown). The image to the right sourced from NZMaths, is based on Pirie and Kieren's growth in understanding model of the 'back and forth' nature of how students develop understanding from the known to the unknown.

A (scope and) sequence should:

- reflect the conceptual needs of your students at this point in time (they need to be evaluated and changed constantly)
- show evidence of connections across sub strands
- address connected content strands that deal with similar concepts within a lesson or within a sequence of lessons (e.g. over a few weeks)
- give teachers an overarching structure to guide immediate planning
- where possible, be written to address the upcoming half- term or term teaching and learning cycle

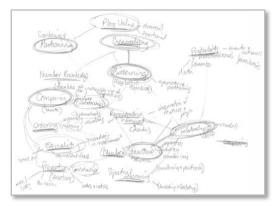
NESA states that for their registration process as evidence of compliance schools need to provide "scope and sequence of learning/units of work in relation to outcomes of NESA syllabus for each KLA for each Year" (page 10). Note: Most schools have a set, wider grade or school-based scope and sequence, you can use the content clusters within those parameters to guide what conceptual understandings you focus on for your students. They show where you can make connections between the sub strands that are listed in the school's scope and sequence.

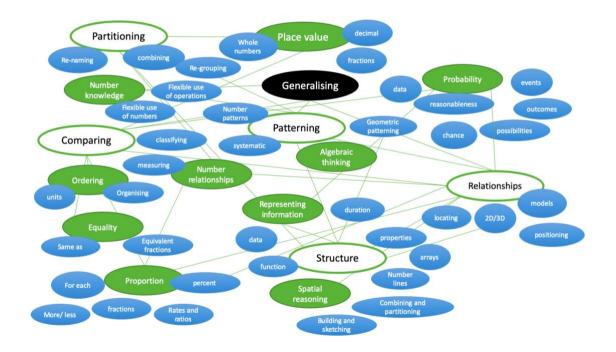




Mind map of big ideas and smaller concept connections

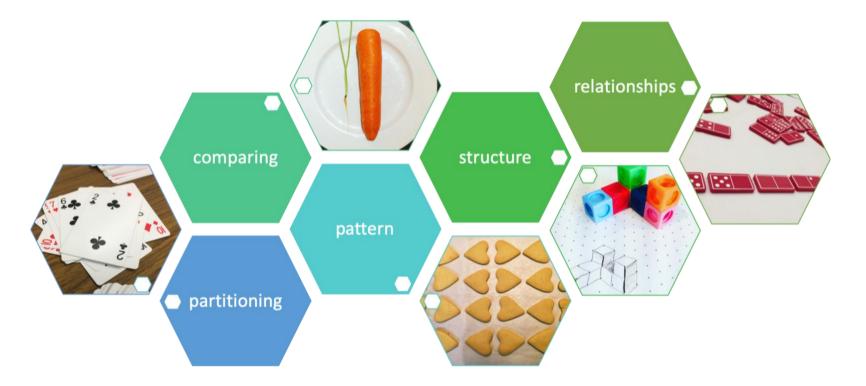
To assist with how these clusters fit into the larger picture of mathematics, what many researchers refer to as 'Big ideas' or important concepts (Askew, 2013; Boaler, 2017; Charles, 2005; Clarke, Clarke & Sullivan, 2012; Hurst & Hurrell, 2014; Siemon, Bleckly & Neal, 2012; Tout & Spithill, 2015), I had a go at thinking holistically about *"What are the main concepts or 'knowledge actions' students need?"* Here is my 'messy' thinking, then a more organised way of linking these ideas together are illustrated on the following pages.







Big ideas simplified



I then thought about these important concepts 'big ideas', the smaller 'knowledge actions' within them, and how the Content Clusters fit under each of these concepts, noting that some clusters align with more than one big idea.



Big ideas and smaller 'knowledge actions'

Partitioning	Pattern	Comparing	Structure	Relationships
 Combining Part-whole Place value Modelling Whole numbers Decimals Fractions 	 Geometric Number Algebraic Generalising Predicting 	 Equality (with numbers and measurement) Ordering Proportion (fractions, percent, rates, ratios) Magnitude Estimating 	 Number Arrays Shape Measuring Spatial Building and sketching Representing features (shape, data) 	 Number Additive and multiplicative 2D and 3D Probability Possibilities (chance) Data Locating, positioning Part-whole

These are just my ideas, Charles (2005) in his paper recognises that in developing deeper understanding of big ideas it might be helpful for teachers to "decide to modify or build your own" (p. 11). He also stated that:

"In working with colleagues on the development of this paper I am rather certain that it is not possible to get one set of Big Ideas and Understandings that all mathematicians and mathematics educators can agree on. Fortunately, I do not think it's necessary to reach a consensus in this regard. Use the Big Mathematical Ideas and Understandings presented here as a starting point for the conversations they are intended to initiate" (p. 9)



Organisation of Stage 3 clusters (updated)

In this update I have reduced the repetition of clusters and now simply have all the clusters included once (they are no longer repeated under substrand headings). A few clusters have been revised (Cluster 3, 11 and 19) to add in other connections that have arisen, specifically time concepts. Where appropriate, clusters have been given the same or similar names as concepts from other Stages to help make connections, show concepts that develop, and to assist with multi-stage planning. This version also includes a visual overview of the clusters mapped to the NSW outcomes they address to assist with planning and programming. A list of cluster titles is also included so teachers can see 'at a glance' the types of concepts the clusters explore. There is no set time for how long each cluster may take to explore with students, it could be 2 weeks per cluster or 3-4 weeks. Clusters may be repeated, merged or omitted (please see these are examples). Decisions about how the clusters are arranged and implemented should be made by teachers at a school/grade/classroom level based on students' needs, abilities, and interests.

References

Askew, M. (2013). Big ideas in primary mathematics: Issues and directions. *Perspectives in Education*, *31*(3), 5-18. Charles, R. I., & Carmel, C. A. (2005). Big ideas and understandings as the foundation for elementary and middle school mathematics. *Journal of Mathematics Education*, *7*(3), 9-24. Clarke, D. M., Clarke, D. J., & Sullivan, P. (2012). Important ideas in mathematics: What are they and where do you get them? *Australian Primary Mathematics Classroom*, *17*(3), 13. Hurst, C., & Hurrell, D. (2014). Developing the big ideas of number. *International Journal of Educational Studies in Mathematics*, *1*(2), 1-18. Mathematics K-10 Syllabus outcomes © NSW Education Standards Authority (NESA) for and on behalf of the Crown in right of the State of New South Wales, 2012. Pirie, S., & Kieren, T. (1994). Growth in mathematical understanding: How can we characterise it and how can we represent it? *Educational Studies in Mathematics*, *26*(2/3), 165-190. doi:10.1007/BF01273662 Siemon, D., Bleckly, J., & Neal, D. (2012). Working with the big ideas in number and the Australian Curriculum: Mathematics. *2012). Engaging the Australian National Curriculum: Mathematics*–*Perspectives from the Field. Online Publication: Mathematics Education Research Group of Australasia*, 19-45. Tout, D. & Spithill, J. (2015). Big Ideas in Mathematics Teaching. *The Research Digest, QCT*, *2015 (11)*

What is mathematical beauty Jo Boaler (Youcubed)

Page 7 of 26

Clusters mapped to big ideas

Primary Learning

•Co

Partitioning
ntent Cluster 1: Place value

•Content Cluster 5: Partitioning •Content Cluster 6: Flexible strategies for operating with numbers

•Content Cluster 7: A variety of strategies can be applied to solve word problems

•Content Cluster 8: Multiples can be visually represented as an array

Content Cluster 11: Number relationships – converting
Content Cluster 12: Money uses a many-to-one scale
Content Cluster 17: A fraction is

•Content Cluster 17: A fraction is a number

Pattern

•Content Cluster 2: Representing numbers

•Content Cluster 8: Multiples can be visually represented as an array

Content Cluster 13: The 'equals sign' means "the same as"
Content Cluster 14: Numbers

can be represented using pairs •Content Cluster 15: Patterns repeat or grow

•Content Cluster 16: Patterns can be represented geometrically

Comparing

•Content Cluster 3: Comparing quantities – linear

•Content Cluster 4: Comparing quantities – area/volume/mass •Content Cluster 9:

Reasonableness of solutions can be checked

•Content Cluster 10: Benchmark numbers can be used to estimate quantities

•Content Cluster 11: Number relationships – converting •Content Cluster 13: The 'equals

sign' means "the same as" •Content Cluster 19: Fractions as a measure

•Content Cluster 21: Time can be measured and compared

•Content Cluster 22: Numbers and quantities can be compared using scale

•Content Cluster 25: Objects can be measured and compared •Content Cluster 26: Shapes can

•Content Cluster 20: Shapes can be measured and compared •Content Cluster 27: Shape and

objects are classified
Content Cluster 29: Information can be collected, analysed and

interpreted •Content Cluster 31: Events can be predicted, compared, and analysed

Structure

 Content Cluster 1: Place value Content Cluster 2: Representing numbers •Content Cluster 4: Comparing quantities – area/volume/mass Content Cluster 5: Partitioning Content Cluster 8: Multiples can be visually represented as an arrav Content Cluster 15: Patterns repeat or grow •Content Cluster 16: Patterns can be represented geometrically •Content Cluster 23: Measurements are approximations •Content Cluster 24: The multiplicative structure •Content Cluster 28: Grid references and coordinates can be used for locating and positioning •Content Cluster 30: Information can be presented visually Content Cluster 32: Probabilities of events can be described in a range of 0-1

Relationships

https://primarylearning.com.au

•Content Cluster 1: Place value Content Cluster 6: Flexible strategies for operating with numbers Content Cluster 11: Number relationships – converting Content Cluster 12: Money uses a many-to-one scale Content Cluster 13: The 'equals sign' means "the same as" •Content Cluster 14: Numbers can be represented using pairs •Content Cluster 17: A fraction is a number Content Cluster 18: Fractions represent division •Content Cluster 20: Fractions as an operator •Content Cluster 22: Numbers and quantities can be compared using scale •Content Cluster 28: Grid references and coordinates can be used for locating and positioning Content Cluster 32: Probabilities of events can be described in a range of 0-1



Stage 3 Overview of Content Clusters

Content Cluster 1: Place value (numbers can be regrouped and renamed – partitioning) Content Cluster 2: Representing numbers (numbers can be represented, ordered and compared based on their place value) Content Cluster 3: Comparing quantities – linear focus (numbers can be compared based on size and place value) Content Cluster 4: Comparing quantities - area/volume/mass focus (numbers can be compared based on size and place value) Content Cluster 5: Partitioning: Part-whole number knowledge (numbers can be partitioned in multiple ways) Content Cluster 6: Flexible strategies for operating with numbers (numbers can be partitioned to assist with computation) Content Cluster 7: A variety of strategies can be applied to solve word problems Content Cluster 8: Multiples can be visually represented as an array ('for each' number structure) Content Cluster 9: Reasonableness of solutions can be checked using estimation Content Cluster 10: Benchmark numbers can be used to estimate quantities (how much/how many) Content Cluster 11: Number relationships – converting (e.g. one thousand can be regrouped as 10 hundreds, 100 tens, or 1000 ones) Content Cluster 12: Money uses a many-to-one scale (link to place value e.g. 100 cents is equal to \$1) Content Cluster 13: The 'equals sign' means "the same as" (equality and inequality) Content Cluster 14: Numbers can be represented using pairs to explore odd and even properties Content Cluster 15: Patterns repeat or grow and future terms can be predicted (number structure) Content Cluster 16: Patterns can be represented geometrically Content Cluster 17: A fraction is a number (that represents a relationship between parts and the whole) Content Cluster 18: Fractions represent division (number relationships) Content Cluster 19: Fractions as a measure Content Cluster 20: Fractions as an operator Content Cluster 21: Time can be measured and compared in hours, minutes and seconds (relating 12 to 24 hour time)



Stage 3 Overview of Content Clusters cont.

Content Cluster 22: Numbers and quantities can be compared using scale (links to proportionality) Content Cluster 23: Measurements are approximations and can be represented using formal units Content Cluster 24: The multiplicative structure (row and column) can be applied to measure area and volume Content Cluster 25: Objects can be measured and compared through different representations Content Cluster 26: Shapes can be measured and compared through different representations Content Cluster 27: Shape and objects are classified based on their properties Content Cluster 28: Grid references and coordinates can be used for locating and positioning Content Cluster 29: Information can be collected, analysed and interpreted using numbers (collecting data) Content Cluster 30: Information can be presented visually to convey meaning (data representations and exploring bias) Content Cluster 31: Events can be predicted, compared, and analysed based on probability Content Cluster 32: Probabilities of events can be described in a range of 0 – 1 (probabilities as fractions of a whole)



Stage 3 Content Cluster outcome mapping

	1 Place value	2 Representing numbers	3 Comparing quantities – linear	f 4 Comparing quantities – area/volume/mass	5 Partitioning: Part-whole number	6 Flexible strategies for operating	7 A variety of strategies can be	8 Multiples can be visually	9 Reasonableness of solutions:	10 Benchmark numbers can be used to est	11 Number relationships – converting	12 Money uses a many-to-one scale	13 The 'equals sign' means 'the same as'	14 Numbers can be represented using pairs	15 Patterns repeat or grow	16 Patterns can be represented	17 A fraction is a number	18 Fractions represent division	19 Fractions as a measure	20 Fractions as an operator	21 Time can be measured and	22 Numbers and quantities can be compared: scale	23 Measurements are approximations	The multiplicative structure	25 Objects can be measured and compared	26 Shapes can be measured and	27 Shape and objects are classified	28 Grid references and coordinates	29 Information can be collected, analysed	30 Information can be presented visually	31 Events can be predicted, compared	32 Probabilities of events: range of 0 – 1
Whole Number MA3-4NA																																
Add & Sub MA3-5NA																																
Multi & Div MA3-6NA																																
Frac & Dec MA3-7NA																																
Pat & Alg MA3-8NA																																
Length MA3-9MG																																
Area MA3-10MG																																
Vol & Cap MA3-11MG																																
Mass MA3-12MG																																
Time MA3-13MG																																
3D Space MA3-14MG																																
2D Space MA3-15MG																																
Angles MA3-16MG																																
Position MA3-17MG																																
Data MA3-18SP																																
Chance MA3-19SP																																

Page 10 of 26



Content Cluster 1: Place value (numbers can be regrouped and renamed – partitioning)									
Whole Numbers 1 MA3-4NA	Fractions and Decimals 1 MA3-7NA	Fractions and Decimals 2 MA3-7NA							
State the place value of digits in numbers of any size	Apply the place value system to represent	Multiply and divide decimals by 10, 100							
Record numbers of any size using expanded notation	thousandths as decimals	and 1000							
Whole Numbers 2 MA3-4NA	Express mixed numerals as improper fractions	Write fractions in their 'simplest form'							
Identify and describe prime and composite numbers	and vice versa								

Content Cluster 2: Representing numbers (numbers can be represented, ordered and	nd compared based on their place value)
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Whole Numbers 1 MA3-	Fractions and Decimals 1	Fractions and Decimals	Length 2 MA3-9MG	Volume and Capacity 2	Mass 2 MA3-12MG
4NA	MA3-7NA	2 MA3-7NA	Record lengths and	MA3-11MG	Record mass using
Read, write and order	Compare and order unit	Represent, compare	distances using decimal	Record volumes and	decimal notation to
numbers of any size	fractions with	and order fractions with	notation to three decimal	capacities using	three decimal places
Whole Numbers 2 MA3-	denominators	denominators	places	decimal notation to	
4NA	2, 3, 4, 5, 6, 8, 10, 12	2, 3, 4, 5, 6, 8, 10, 12		three decimal places	
Recognise the location of	and 100	and 100			
negative numbers in relation	Compare, order and				
to zero on a number line	represent decimals with				
	up to three decimal places				



Content Cluster 3: Comparing quantities – linear focus (numbers can be compared based on size and place value)										
Fractions and Decimals 1 MA3- 7NA	Length 1 MA3-9MG Use the kilometre to measure lengths	Length 2 MA3-9MG Record lengths and	Volume and Capacity 2 MA3- 11MG	Time 1MA3-13MG Convert between 12- and						
Compare and order unit	and distances	distances using decimal	Record volumes and capacities	24-hour time						
fractions with denominators	Select and use appropriate	notation to three decimal	using decimal notation to three							
2, 3, 4, 5, 6, 8, 10, 12 and 100	instruments and units to measure	places	decimal places							
Compare, order and represent	lengths	Convert between	Convert between millilitres and							
decimals with up to three	Record lengths and distances using	kilometres, metres,	litres							
decimal places	the abbreviations km, m, cm and mm	centimetres and millimetres								

Fractions and Decimals 1	Area 1 MA3-10MG	Volume and Capacity 1 MA3-	Mass 1 MA3-12MG
MA3-7NA	Recognise the need for	11MG	Recognise the need for tonnes to measure mass
Compare and order unit	square kilometres and	Use cubic centimetres and cubic	Record masses using the abbreviations t, kg and g
fractions with denominators	hectares to measure area	metres to measure and estimate	Select and use appropriate instruments and units to measure mass
2, 3, 4, 5, 6, 8, 10, 12	Record areas using the	volumes	Solve problems involving mass
and 100	abbreviations km2 and ha	Select and use appropriate units	Mass 2 MA3-12MG
Compare, order and		to measure volume	Record mass using decimal notation to three decimal places
represent decimals with		Record volumes using the	Convert between tonnes, kilograms and grams
up to three decimal places		abbreviations cm3 and m3	



Content Cluster 5: Partitioning: Part-whole number knowledge (numbers can be partitioned in multiple ways)										
Whole Numbers 1 MA3-4NA	Fractions and Decimals 1 MA3-7NA	Fractions and Decimals 2 MA3-7NA	Multiplication and Division 1 MA3-6NA							
Record numbers of any size using	Compare and order unit fractions with	Represent, compare and order	Use and record a range of mental and							
expanded notation	denominators 2, 3, 4, 5, 6, 8, 10, 12	fractions with denominators	written strategies to divide numbers with							
Whole Numbers 2 MA3-4NA	and 100	2, 3, 4, 5, 6, 8, 10, 12 and 100	three or more digits by a one-digit							
Identify and describe prime and	Express mixed numerals as improper	Write fractions in their 'simplest	operator, including problems that result							
composite numbers	fractions and vice versa	form'	in a remainder							

Content Cluster 6: Flexible strategies for operating with numbers (numbers can be partitioned to assist with computation)									
Multiplication and Division 1 MA3-6NA	Fractions and Decimals 1 MA3-7NA								
Use and record a range of mental and	Model and represent strategies to add and subtract fractions with the same								
written strategies to multiply by one- and	denominator								
two-digit operators	Fractions and Decimals 2 MA3-7NA								
Use and record a range of mental and	Add and subtract fractions, included mixed numerals, with the same or related								
written strategies to divide numbers with	denominators								
three or more digits by a one-digit operator,	Use mental, written and calculator strategies to add and subtract decimals with up to								
including problems that result in a remainder	three decimal places								
	Use mental, written and calculator strategies to multiply decimals by one- and two-digit								
	whole numbers								
	Use mental, written and calculator strategies to divide decimals by one-digit whole								
	numbers								
	Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators Use and record a range of mental and written strategies to divide numbers with three or more digits by a one-digit operator,								



Content Cluster 7: A variety	Content Cluster 7: A variety of strategies can be applied to solve word problems										
Addition and Subtraction 1 MA3-5NA	Addition and Subtraction 2 MA3-5NA Select and apply efficient mental, written and	Multiplication and Division 1 MA3-6NA Solve word problems and record the	Fractions and Decimals 2 MA3-7NA								
Solve word problems and	calculator strategies to solve word problems	strategy used	Solve word problems involving								
record the strategy used,	and record the strategy used	Multiplication and Division 2 MA3-6NA	fractions and decimals,								
including problems involving money		Select and apply efficient mental, written and calculator strategies to solve word problems and	including money problems								
		record the strategy used									

Content Cluster 8: Multiples can be visually represented as an array ('for each' number structure)										
Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators Use and record a range of mental and written strategies to divide numbers with three or more digits by a one-digit operator, including problems that result in a remainder	Multiplication and Division 2 MA3-6NA Select and apply efficient mental, written and calculator strategies to solve word problems and record the strategy used	Area 1 MA3-10MG Develop a strategy to find areas of rectangles (including squares) and record the strategy in words Area 2 MA3-10MG Develop a strategy to find areas of triangles and record the strategy in words	Volume and Capacity 2 MA3- 11MG Develop a strategy to find volumes of rectangular prisms and record the strategy in words	Patterns and Algebra 2 MA3-8NA Continue, create, record and describe geometric and number patterns in words						



Content Cluster 9: Reasonableness of solutions can be checked using estimation				
Addition and Subtraction 1 MA3-5NA	Multiplication and Division 1 MA3-6NA Solve word problems and record the	Multiplication and Division 2 MA3-6NA Select and apply efficient mental, written and	Fractions and Decimals 2 MA3-7NA	
Use estimation to check answers to calculations	strategy used Use estimation to check answers to	calculator strategies to solve word problems and record the strategy used	Solve word problems involving fractions and decimals,	
Solve word problems and record the strategy used,	calculations		including money problems	
including problems involving money				

Content Cluster 10: Benchmark numbers can be used to estimate quantities (how much/how many)						
Addition and Subtraction 1 Multiplication and Fractions and Decimals Volume and Capacity 1 MA3-11MG Angles 1 MA3-16MG						
MA3-5NA	Division 1 MA3-6NA	2 MA3-7NA	Use cubic centimetres and cubic metres to	Measure, compare and estimate		
Use estimation to check	Solve word problems and	Make connections	measure and estimate volumes	angles in degrees (up to 360°)		
answers to calculations	record the strategy used	between equivalent	Select and use appropriate units to measure	Record angle measurements		
	Use estimation to check	percentages, fractions	volume	using the symbol for degrees (°)		
	answers to calculations	and decimals				



Whole Numbers 1 MA3-4NA	Time 1MA3-13MG	Fractions and Decimals 1 MA3-7NA	Length 2 MA3-9MG	Volume and Capacity 2	Mass 2 MA3-12MC
Read, write and order numbers	Convert between 12-	Apply the place value system to	Convert between	MA3-11MG	Convert between
of any size	and 24-hour time	represent thousandths as decimals	kilometres, metres,	Convert between	tonnes, kilograms
State the place value of digits in	Determine and	Fractions and Decimals 2 MA3-7NA	centimetres and	millilitres and litres	and grams
numbers of any size	compare the duration	Multiply and divide decimals by	millimetres		
Record numbers of any size	of events	10, 100 and 1000			
using expanded notation					

Content Cluster 12: Money uses a many-to-one scale (link to place value e.g. 100 cents is equal to \$1)					
Addition and Subtraction 1 MA3-5NA Multiplication and Division 1 MA3-6NA Fractions and Decimals 2 MA3-7NA					
Solve word problems and record the strategy used,	Solve word problems and record the	Solve word problems involving fractions and decimals, including money			
including problems involving money	strategy used	problems			
Create a simple budget	Interpret remainders in division problems	Use mental, written and calculator strategies to calculate 10%, 25%			
		and 50% of quantities, including as discounts			

Content Cluster 13: The 'equals sign' means "the same as" (equality and inequality)				
Multiplication and Division 2 MA3-6NA Patterns and Algebra 1 MA3-8NA Fractions and Decimals 2 MA3-7NA				
Recognise and use grouping symbols	Find missing numbers in number sentences involving	Determine, generate and record equivalent fractions		
Apply the order of operations in calculations	multiplication or division on one or both sides of the equals	Make connections between equivalent percentages, fractions		
	sign	and decimals		



Content Cluster 14: Numbers can be represented using pairs to explore odd and even properties				
Patterns and Algebra 1 MA3-8NA Whole Numbers 1 MA3-4NA				
Identify, continue create and describe increasing and decreasing number	Determine factors and multiples of whole numbers			
patterns with fractions, decimals and whole numbers	Whole Numbers 2 MA3-4NA			
	Identify and describe prime and composite numbers			
	Model and describe square and triangular numbers			

Content Cluster 15: Patterns repeat or grow and future terms can be predicted (number structure)				
Patterns and Algebra 1 MA3- 8NA Identify, continue create and describe increasing and decreasing number patterns with fractions, decimals and whole numbers	Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators	Fractions and Decimals 1 MA3-7NA Model and represent strategies to add and subtract fractions with the same denominator Fractions and Decimals 2 MA3-7NA Use mental, written and calculator strategies to add and subtract decimals with up to three decimal places Use mental, written and calculator strategies to multiply decimals by one- and two-digit whole numbers Use mental, written and calculator strategies to divide decimals by one-digit whole numbers	Whole Numbers 1 MA3-4NA Read, write and order numbers of any size Whole Numbers 2 MA3-4NA Model and describe square and triangular numbers	Addition and Subtraction 1 MA3- 5NA Select and apply efficient mental, written and calculator strategies for addition and subtraction of numbers of any size



Content Cluster 16: Patterns can be represented geometrically				
Patterns and Algebra 2	Multiplication and	Two-Dimensional Space 1 MA3-15MG	Whole Numbers 1 MA3-4NA	Addition and Subtraction 1 MA3-
MA3-8NA	Division 1 MA3-6NA	Classify and draw regular and irregular	Read, write and order	5NA
Continue, create, record	Use and record a	two-dimensional shapes from descriptions	numbers of any size	Select and apply efficient
and describe geometric	range of mental and	of their features	Whole Numbers 2 MA3-4NA	mental, written and calculator
and number patterns in	written strategies to	Use the terms 'translate', 'reflect' and 'rotate'	Model and describe square	strategies for addition and
words	multiply by one- and	to describe transformations of shapes	and triangular numbers	subtraction of numbers of any
Determine the rule for	two-digit operators	Two-Dimensional Space 2 MA3-15MG		size
geometric and number		Identify, use and describe combinations		
patterns in words and		of translations, reflections and rotations		
use the rule to calculate				
values				

Content Cluster 17: A fraction is a number (that represents a relationship between parts and the whole)				
Fractions and Decimals 1 MA3-7NA	Fractions and Decimals 2 MA3-7NA	Whole Numbers 2 MA3-4NA		
Compare and order unit fractions with	Represent, compare and order fractions with denominators	Read, write and order numbers of any		
denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100	2, 3, 4, 5, 6, 8, 10, 12 and 100	size		
Express mixed numerals as improper fractions	Determine, generate and record equivalent fractions	State the place value of digits in		
and vice versa	Write fractions in their 'simplest form'	numbers of any size		
	Make connections between equivalent percentages, fractions and	Record numbers of any size using		
	decimals	expanded notation		



Content Cluster 18: Fractions represent division (number relationships)				
Fractions and Decimals 1 MA3- 7NA	Fractions and Decimals 2 MA3-7NA Represent, compare and order fractions	Multiplication and Division 1 MA3-6NA Use and record a range of mental and	Patterns and Algebra 1 MA3-8NA Identify, continue create and describe	
Compare and order unit fractions with denominators	with denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100	written strategies to divide numbers with three or more digits by a one-digit operator,	increasing and decreasing number patterns with fractions, decimals and whole numbers	
2, 3, 4, 5, 6, 8, 10, 12 and 100 Express mixed numerals as	Determine, generate and record equivalent fractions	including problems that result in a remainder Interpret remainders in division problems		
improper fractions and vice versa	Write fractions in their 'simplest form'			

Content Cluster 19: Fractions as a measure				
Fractions and Decimals 1 MA3-	Length 1 MA3-9MG	Area 1 MA3-10MG	Time 1MA3-13MG	
7NA	Record lengths and distances using the	Recognise the need for square kilometres and	Convert between 12- and	
Model and represent strategies to	abbreviations km, m, cm and mm	hectares to measure area	24-hour time	
add and subtract fractions with the	Find perimeters of common two-	Record areas using the abbreviations km ₂ and ha	Time 2 MA3-13MG	
same denominator	dimensional shapes and record the	Develop a strategy to find areas of rectangles	Interpret and use	
Fractions and Decimals 2 MA3-	strategy	(including squares) and record the strategy in words	timetables	
7NA	Length 2 MA3-9MG	Area 2 MA3-10MG		
Add and subtract fractions,	Convert between kilometres, metres,	Develop a strategy to find areas of triangles and		
included mixed numerals, with the	centimetres and millimetres	record the strategy in words		
same or related denominators	Solve problems involving length and	Solve problems involving areas of rectangles		
	perimeter	(including squares) and triangles		



Content Cluster 20: Fractions as an operator				
Fractions and Decimals 2 MA3-7NA Multiply fractions by whole numbers Find a simple fraction of a quantity Solve word problems involving fractions and decimals, including money problems Make connections between equivalent percentages, fractions and decimals Use mental, written and calculator strategies to calculate	Addition and Subtraction 1 MA3- 5NA Solve word problems and record the strategy used, including problems involving money Create a simple budget	Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators	Area 2 MA3-10MG Solve problems involving areas of rectangles (including squares) and triangles	
10%, 25% and 50% of quantities, including as discounts				

Content Cluster 21: Time can be measured and compared in hours, minutes and seconds (relating 12 to 24 hour time)				
Time 1MA3-13MG	Time 2 MA3-13MG	Fractions and Decimals 1 MA3-7NA	Addition and Subtraction 2 MA3-5NA	
Convert between 12- and 24-hour time	Interpret and use timetables	Model and represent strategies to	Select and apply efficient mental, written and	
Determine and compare the duration		add and subtract fractions with the	calculator strategies to solve word problems and	
of events		same denominator	record the strategy used	



Multiplication and	Length 1 MA3-9MG	Position MA3-17MG	Data 1 MA3-18SP	Time 2 MA3-	Two-Dimensional
Division 1 MA3-6NA	Select and use appropriate	Use grid-referenced maps to	Construct data displays,	13MG	Space 1 MA3-
Use and record a	instruments and units to measure	locate and describe positions	including tables, column graphs,	Draw and	15MG
range of mental and	lengths	Follow a sequence of directions,	dot plots and line graphs,	interpret	Make and compare
written strategies to	Record lengths and distances using	including compass directions, to	appropriate for the data type	timelines using	enlargements of
multiply by one- and	the abbreviations km, m, cm and mm	find a particular location on a map	Describe and interpret data	a given scale	shapes/pictures
two-digit operators	Length 2 MA3-9MG	Describe routes using landmarks	presented in tables, column		
	Convert between kilometres, metres,	and directional language	graphs, dot plots and line graphs		
	centimetres and millimetres				

Content Cluster 23: Measurements are approximations and can be represented using formal units

Length 1 MA3-9MG	Area 1 MA3-10MG	Volume and Capacity 1 MA3-	Mass 1 MA3-12MG	Angles 1 MA3-16MG
Record lengths and	Record areas using	11MG	Recognise the need for tonnes to	Recognise the need for formal units to
distances using the	the abbreviations	Record volumes using the	measure mass	measure angles
abbreviations km, m, cm	km2 and ha	abbreviations cm3 and m3	Record masses using the abbreviations t,	Record angle measurements using the
and mm		Volume and Capacity 2 MA2-	kg and g	symbol for degrees (°)
Length 2 MA3-9MG		11MG	Distinguish between 'gross mass' and	Construct angles using a protractor
Record lengths and		Record volumes and capacities	'net mass'	(up to 360°)
distances using decimal		using decimal notation to three	Mass 2 MA3-12MG	Describe angle size in degrees for each
notation to three decimal		decimal places	Record mass using decimal notation to	angle classification
places		Convert between millilitres and	three decimal places	
		litres		



Content Cluster 24: The multiplicative structure (row and column) can be applied to measure area and volume					
Multiplication and	Fraction and Decimals 2	Area 1 MA3-10MG Develop a strategy to find areas of	Volume and Capacity 2 MA3-	Three-Dimensional Space 2 MA3-	
Division 1 MA3-6NA	MA3-7NA		11MG	14MG	
Use and record a range	Use mental, written and	rectangles (including squares) and	Develop a strategy to find	Construct prisms and pyramids	
of mental and written	calculator strategies	record the strategy in words	volumes of rectangular prisms	using a variety of materials, and	
strategies to multiply by	to multiply decimals by one-	Area 2 MA3-10MG	and record the strategy	given drawings from different	
one- and two-digit operators	and two-digit whole numbers	Develop a strategy to find areas of triangles and record the strategy in words	in words	views	

Content Cluster 25: Objects can be measured and compared through different representations				
Three-dimensional Space 1 MA3-14MG	Volume and Capacity 1 MA3-11MG	Multiplication and Division 1 MA3-6NA		
Describe and compare properties of prisms and	Use cubic centimetres and cubic metres to measure and	Use and record a range of mental and written		
pyramids in terms of their faces, edges and vertices	estimate volumes	strategies to multiply by one- and two-digit		
Connect three-dimensional objects with their nets	Select and use appropriate units to measure volume	operators		
Three-Dimensional Space 2 MA3-14MG	Volume and Capacity 2 MA3-11MG			
Construct prisms and pyramids using a variety of	Connect volume and capacity and their units			
materials, and given drawings from different views	of measurement			
	Develop a strategy to find volumes of rectangular prisms			
	and record the strategy in words			



opposite angles'

Use known angle results to find

unknown angles in diagrams

Identify and name parts of circles

Stage 3 Content Clusters

Content Cluster 26: Shapes can be measured and compared through different representations					
Two-Dimensional Space 1 MA3-15MG Identify, name and draw right-angled, equilateral, isosceles and scalene triangles Compare and describe side properties of the special quadrilaterals and special triangles Explore angle properties of the special quadrilaterals and special triangles	Area 1 MA3-10MG Develop a strategy to find areas of rectangles (including squares) and record the strategy in words f Area 2 MA3-10MG Develop a strategy to find areas of triangles and record the strategy in words	Length 1 MA3-9MG Find perimeters of common two- dimensional shapes and record the strategy	Angles 1 MA3-16MG Measure, compare and estimate angles in degrees (up to 360°) Describe angle size in degrees for each angle classification		
-	jects are classified based on their propert	Two-Dimensional Space 2 MA3-	Angles 2 MA3-16MG		
14MG Name prisms and pyramids	dentify, name and draw right-angled, equilateral, sosceles and scalene triangles Compare and describe side properties of the speci	15MG Identify, describe, compare and	Identify and name angle types formed by the intersection of straight lines, including 'angles on a straight line',		
Recognise that prisms have a	quadrilaterals and special triangles	shapes	'angles at a point' and 'vertically		

Explore angle properties of the special quadrilaterals

shapes from descriptions of their features

Identify line and rotational symmetries

Classify and draw regular and irregular two-dimensional

and special triangles

faces, edges and vertices

do not

uniform cross-section and pyramids

Describe and compare properties of

prisms and pyramids in terms of their



Position 1 MA3-17MG Patterns and Algebra 2 MA3- Two-Dimensional Space 1 MA3-15MG Three-Dimensional Space 2					
Use grid-referenced maps to	8NA	Use the terms 'translate', 'reflect' and 'rotate' to describe	14MG		
locate and describe positions	Locate and record the	transformations of shapes	Construct prisms and pyramids		
	coordinates of points in all four	Make and compare enlargements of shapes/pictures	using a variety of materials, and		
	quadrants of the Cartesian plane	Two-Dimensional Space 2 MA3-15MG	given drawings from different view		
		Identify, use and describe combinations of translations,			
		reflections and rotations			

Content Cluster 29: Information can be collected, analysed and interpreted using numbers (collecting data)				
Data 1 MA3-18SP	Data 2 MA3-18SP	Chance 1 MA3-19SP	Addition and Subtraction	Multiplication and Division
Collect categorical and	Interpret and create two-way	List outcomes of chance experiments	1 MA3-5NA	1 MA3-6NA
numerical data by observation	tables	involving equally likely outcomes	Select and apply efficient	Use and record a range
and by survey	Interpret side-by-side column	Chance 2 MA3-19SP	mental, written	of mental and written
Describe and interpret data	graphs	Conduct chance experiments with	and calculator strategies	strategies to divide
presented in tables, column	Compare a range of data displays	both small and large numbers of trials	for addition and	numbers with three or
graphs, dot plots and line	to determine the most appropriate		subtraction of numbers of	more digits by a one-digit
graphs	display for particular sets of data		any size	operator
	Interpret and critically evaluate			
	data presented in digital media and			
	elsewhere			



Content Cluster 30: Information can be presented visually to convey meaning (data representations and exploring bias)				
Data 1 MA3-18SP	Data 2 MA3-18SP	Angles 1 MA3-16MG	Length 1 MA3-9MG	
Construct data displays, including tables,	Interpret and create two-way tables	Construct angles using a protractor	Select and use appropriate	
column graphs, dot plots and line	Compare a range of data displays to	(up to 360°)	instruments and units to measure	
graphs, appropriate for the data type	determine the most appropriate display		lengths	
	for particular sets of data			
Content Cluster 31: Events can be	predicted, compared, and analysed base	d on probability		
Chance 1 MA3-19SP	Chance 2 MA3-19SP	Data 1 MA3-18SP	Data 2 MA3-18SP	
List outcomes of chance experiments	Compare observed frequencies in chance	Collect categorical and numerical data by	Interpret and critically evaluate data	
involving equally likely outcomes	experiments with expected frequencies	observation and by survey	presented in digital media and	
	Conduct chance experiments with both small	Describe and interpret data presented in	elsewhere	

Conduct chance experiments with both small	Describe and interpret data presented in	elsewhere
and large numbers of trials	tables, column graphs, dot plots and line	
	graphs	

Content Cluster 32: Probabilities of events can be described in a range of 0 – 1 (probabilities as fractions of a whole)

Chance 1 MA3-19SP	Chance 2 MA3-19SP	Data 1 MA3-18SP	Fractions and Decimals 2 MA3-7NA
Represent probabilities using fractions	Compare observed frequencies in chance	Collect categorical and numerical	Represent, compare and order fractions with
Recognise that probabilities range from	experiments with expected frequencies	data by observation and by survey	denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100
0 to 1	Represent probabilities using fractions,		Solve word problems involving fractions and
	decimals and percentages		decimals

