## Content Clusters - Stage 3

## Scope and sequencing by conceptual understanding

This is the scope... you create the sequence.
In this resource I provide possible ways of how groups of outcomes and their key ideas can be sequenced together based on the concepts they address. These are just examples and is not an exhaustive list of the clusters you can use to make connections across mathematics. I have used
 the syllabus outcomes, sub strands and the mathematics key ideas document. When teaching for conceptual understanding (not just the knowledge of each sub strand) we need to make clear how the pieces of the mathematical puzzle fit together. To do this, our planning needs to reflect this belief - that mathematics is a complex web of interrelated ideas. For ideas on what these links are, see my Linkages across the syllabus document on the resources section of our website.

The scope of what we teach is described in the syllabus (this is the constant), the sequence of what and how we teach mathematics is a decision for individual teachers (this is the variable). These clusters can be used to create meaningful sequences of learning that focus on concepts and programs that still address common sub strands (across grades or classes) but allow for individual teachers to add additional key ideas or focus on specific aspects of the cluster that students either have misconceptions around or are developing conceptual understanding in. The clusters are numbered but are not written in teaching order. These clusters may be added to or updated in the future and newer versions will be released.

## Primary Learning

These clusters highlight the concept or main idea that ties each group of outcomes together, assisting teachers in making sense and meaning of the mathematics to students. When we think about the concepts or understandings first, we can think about what misconceptions students may have or what aspects of that concept they need next to connect their prior knowledge (the known) to create new knowledge (the unknown). The image to the right sourced from NZMaths, is based on Pirie and Kieren's growth in understanding model of the 'back and forth' nature of how students develop understanding from the known to the unknown.

A (scope and) sequence should:


- reflect the conceptual needs of your students at this point in time (they need to be evaluated and changed constantly)
- show evidence of connections across sub strands
- address connected content strands that deal with similar concepts within a lesson or within a sequence of lessons (e.g. over a few weeks)
- give teachers an overarching structure to guide immediate planning
- where possible, be written to address the upcoming half- term or term teaching and learning cycle

NESA states that for their registration process as evidence of compliance schools need to provide "scope and sequence of learning/units of work in relation to outcomes of NESA syllabus for each KLA for each Year" (page 10). Note: Most schools have a set, wider grade or school-based scope and sequence, you can use the content clusters within those parameters to guide what conceptual understandings you focus on for your students. They show where you can make connections between the sub strands that are listed in the school's scope and sequence.

## Primary

## Mind map of big ideas and smaller concept connections

To assist with how these clusters fit into the larger picture of mathematics, what many researchers refer to as 'Big ideas' or important concepts (Askew, 2013; Boaler, 2017; Charles, 2005; Clarke, Clarke \& Sullivan, 2012; Hurst \& Hurrell, 2014; Siemon, Bleckly \& Neal, 2012; Tout \& Spithill, 2015), I had a go at thinking holistically about "What are the main concepts or 'knowledge actions' students need?" Here is my 'messy' thinking, then a more organised way of linking these ideas together are illustrated on the following pages.


## Big ideas simplified



I then thought about these important concepts 'big ideas', the smaller 'knowledge actions' within them, and how the Content Clusters fit under each of these concepts, noting that some clusters align with more than one big idea.

## Primary

## Big ideas and smaller 'knowledge actions'

| Partitioning | Pattern |  | Comparing |  | Structure |
| :--- | :--- | :--- | :--- | :--- | :--- |

These are just my ideas, Charles (2005) in his paper recognises that in developing deeper understanding of big ideas it might be helpful for teachers to "decide to modify or build your own" (p. 11). He also stated that:
"In working with colleagues on the development of this paper I am rather certain that it is not possible to get one set of Big Ideas and Understandings that all mathematicians and mathematics educators can agree on. Fortunately, I do not think it's necessary to reach a consensus in this regard. Use the Big Mathematical Ideas and Understandings presented here as a starting point for the conversations they are intended to initiate" (p. 9)

## Primary Learning

## Organisation of Stage 3 clusters (updated)

In this update I have reduced the repetition of clusters and now simply have all the clusters included once (they are no longer repeated under substrand headings). A few clusters have been revised (Cluster 3,11 and 19) to add in other connections that have arisen, specifically time concepts. Where appropriate, clusters have been given the same or similar names as concepts from other Stages to help make connections, show concepts that develop, and to assist with multi-stage planning. This version also includes a visual overview of the clusters mapped to the NSW outcomes they address to assist with planning and programming. A list of cluster titles is also included so teachers can see 'at a glance' the types of concepts the clusters explore. There is no set time for how long each cluster may take to explore with students, it could be 2 weeks per cluster or $3-4$ weeks. Clusters may be repeated, merged or omitted (please see these are examples). Decisions about how the clusters are arranged and implemented should be made by teachers at a school/grade/classroom level based on students' needs, abilities, and interests.

## References

Askew, M. (2013). Big ideas in primary mathematics: Issues and directions. Perspectives in Education, 31(3), 5-18.
Charles, R. I., \& Carmel, C. A. (2005). Big ideas and understandings as the foundation for elementary and middle school mathematics. Journal of Mathematics Education, 7(3), 9-24.
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Hurst, C., \& Hurrell, D. (2014). Developing the big ideas of number. International Journal of Educational Studies in Mathematics, 1(2), 1-18.
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Tout, D. \& Spithill, J. (2015). Big Ideas in Mathematics Teaching. The Research Digest, QCT, 2015 (11)
What is mathematical beauty Jo Boaler (Youcubed)

## Primary

Learning

## Clusters mapped to big ideas

## Partitioning

-Content Cluster 1: Place value -Content Cluster 5: Partitioning -Content Cluster 6: Flexible strategies for operating with numbers
-Content Cluster 7: A variety of strategies can be applied to solve word problems
-Content Cluster 8: Multiples can be visually represented as an array
-Content Cluster 11: Number relationships - converting
-Content Cluster 12: Money uses a many-to-one scale
-Content Cluster 17: A fraction is a number

## Pattern

-Content Cluster 2: Representing numbers
-Content Cluster 8: Multiples can be visually represented as an array
-Content Cluster 13: The 'equals sign' means "the same as"
-Content Cluster 14: Numbers can be represented using pairs -Content Cluster 15: Patterns repeat or grow - Content Cluster 16: Patterns can be represented geometrically

## Comparing

-Content Cluster 3: Comparing quantities - linear
-Content Cluster 4: Comparing quantities - area/volume/mass -Content Cluster 9:
Reasonableness of solutions can be checked
-Content Cluster 10: Benchmark numbers can be used to estimate quantities
-Content Cluster 11: Number relationships - converting -Content Cluster 13: The 'equals -Content Cluster 13: The 'equ
sign' means "the same as" -Content Cluster 19: Fractions as a measure
-Content Cluster 21: Time can be measured and compared -Content Cluster 22: Numbers and quantities can be compared using scale
-Content Cluster 25: Objects can be measured and compared -Content Cluster 26: Shapes can be measured and compared -Content Cluster 27: Shape and objects are classified
-Content Cluster 29: Information can be collected, analysed and interpreted
-Content Cluster 31: Events can be predicted, compared, and analysed

## Structure

-Content Cluster 1: Place value -Content Cluster 2: Representing numbers
-Content Cluster 4: Comparing quantities - area/volume/mass -Content Cluster 5: Partitioning -Content Cluster 8: Multiples can be visually represented as an array
-Content Cluster 15: Patterns repeat or grow
-Content Cluster 16: Patterns can be represented geometrically -Content Cluster 23: Measurements are approximations
-Content Cluster 24: The multiplicative structure
Content Cluster 28: Grid references and coordinates can be used for locating and positioning
-Content Cluster 30: Information can be presented visually -Content Cluster 32: Probabilities of events can be described in a range of 0-1

## Relationships

-Content Cluster 1: Place value - Content Cluster 6: Flexible strategies for operating with numbers
-Content Cluster 11: Number relationships - converting -Content Cluster 12: Money uses a many-to-one scale
-Content Cluster 13: The 'equals sign' means "the same as" -Content Cluster 14: Numbers can be represented using pairs Content Cluster 17: A fraction is a number
-Content Cluster 18: Fractions represent division
-Content Cluster 20: Fractions as an operator
-Content Cluster 22: Numbers and quantities can be compared using scale
-Content Cluster 28: Grid
references and coordinates can be used for locating and positioning
Content Cluster 32: Probabilities of events can be described in a range of 0-1

## Primary

Learning

## Stage 3 Overview of Content Clusters

Content Cluster 1: Place value (numbers can be regrouped and renamed - partitioning)
Content Cluster 2: Representing numbers (numbers can be represented, ordered and compared based on their place value)
Content Cluster 3: Comparing quantities - linear focus (numbers can be compared based on size and place value)
Content Cluster 4: Comparing quantities - area/volume/mass focus (numbers can be compared based on size and place value)
Content Cluster 5: Partitioning: Part-whole number knowledge (numbers can be partitioned in multiple ways)
Content Cluster 6: Flexible strategies for operating with numbers (numbers can be partitioned to assist with computation)
Content Cluster 7: A variety of strategies can be applied to solve word problems
Content Cluster 8: Multiples can be visually represented as an array ('for each' number structure)
Content Cluster 9: Reasonableness of solutions can be checked using estimation
Content Cluster 10: Benchmark numbers can be used to estimate quantities (how much/how many)
Content Cluster 11: Number relationships - converting (e.g. one thousand can be regrouped as 10 hundreds, 100 tens, or 1000 ones)
Content Cluster 12: Money uses a many-to-one scale (link to place value e.g. 100 cents is equal to $\$ 1$ )
Content Cluster 13: The 'equals sign' means "the same as" (equality and inequality)
Content Cluster 14: Numbers can be represented using pairs to explore odd and even properties
Content Cluster 15: Patterns repeat or grow and future terms can be predicted (number structure)
Content Cluster 16: Patterns can be represented geometrically
Content Cluster 17: A fraction is a number (that represents a relationship between parts and the whole)
Content Cluster 18: Fractions represent division (number relationships)
Content Cluster 19: Fractions as a measure
Content Cluster 20: Fractions as an operator
Content Cluster 21: Time can be measured and compared in hours, minutes and seconds (relating 12 to 24 hour time)

## Primary

 Learning
## Stage 3 Overview of Content Clusters cont.

Content Cluster 22: Numbers and quantities can be compared using scale (links to proportionality)
Content Cluster 23: Measurements are approximations and can be represented using formal units
Content Cluster 24: The multiplicative structure (row and column) can be applied to measure area and volume
Content Cluster 25: Objects can be measured and compared through different representations
Content Cluster 26: Shapes can be measured and compared through different representations
Content Cluster 27: Shape and objects are classified based on their properties
Content Cluster 28: Grid references and coordinates can be used for locating and positioning
Content Cluster 29: Information can be collected, analysed and interpreted using numbers (collecting data)
Content Cluster 30: Information can be presented visually to convey meaning (data representations and exploring bias)
Content Cluster 31: Events can be predicted, compared, and analysed based on probability
Content Cluster 32: Probabilities of events can be described in a range of $0-1$ (probabilities as fractions of a whole)

Stage 3 Content Cluster outcome mapping

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| Whole Number MA3-4NA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Add \& Sub MA3-5NA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Multi \& Div MA3-6NA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Frac \& Dec MA3-7NA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Pat \& Alg MA3-8NA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Length } \\ & \text { MA3-9MG } \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Area } \\ & \text { MA3-10MG } \\ & \hline \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Vol \& Cap MA3-11MG |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Mass } \\ & \text { MA3-12MG } \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Time <br> MA3-13MG |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { 3D Space } \\ & \text { MA3-14MG } \end{aligned}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2D Space <br> MA3-15MG |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Angles MA3-16MG |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Position MA3-17MG |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Data MA3-18SP |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Chance MA3-19SP |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Stage 3 Content Clusters

Content Cluster 1: Place value (numbers can be regrouped and renamed - partitioning)

## Whole Numbers 1 MA3-4NA

State the place value of digits in numbers of any size Record numbers of any size using expanded notation

Whole Numbers 2 MA3-4NA
Identify and describe prime and composite numbers

Fractions and Decimals 1 MA3-7NA
Apply the place value system to represent thousandths as decimals

Express mixed numerals as improper fractions and vice versa

## Fractions and Decimals 2 MA3-7NA

Multiply and divide decimals by 10, 100 and 1000

Write fractions in their 'simplest form'

## Content Cluster 2: Representing numbers (numbers can be represented, ordered and compared based on their place value)

| Whole Numbers 1 MA34NA <br> Read, write and order numbers of any size <br> Whole Numbers 2 MA34NA <br> Recognise the location of negative numbers in relation to zero on a number line | Fractions and Decimals 1 MA3-7NA <br> Compare and order unit fractions with denominators $2,3,4,5,6,8,10,12$ <br> and 100 <br> Compare, order and represent decimals with up to three decimal places | Fractions and Decimals <br> 2 MA3-7NA <br> Represent, compare and order fractions with denominators $2,3,4,5,6,8,10,12$ and 100 | Length 2 MA3-9MG <br> Record lengths and distances using decimal notation to three decimal places | Volume and Capacity 2 MA3-11MG <br> Record volumes and capacities using decimal notation to three decimal places | Mass 2 MA3-12MG <br> Record mass using decimal notation to three decimal places |
| :---: | :---: | :---: | :---: | :---: | :---: |

## Stage 3 Content Clusters

Content Cluster 3: Comparing quantities - linear focus (numbers can be compared based on size and place value)

| Fractions and Decimals 1 MA3- | Length 1 MA3-9MG | Length 2 MA3-9MG | Volume and Capacity 2 MA3- | Time 1MA3-13MG |
| :--- | :--- | :--- | :--- | :--- |
| 7NA | Use the kilometre to measure lengths | Record lengths and | 11MG |  |
| Compare and order unit | and distances | distances using decimal | Record volumes and capacities | Convert between 12- and |
| fractions with denominators time |  |  |  |  |
| $2,3,4,5,6,8,10,12$ and 100 | Select and use appropriate | instruments and units to measure | places to three decimal | using decimal notation to three <br> decimal places <br> Compare, order and represent <br> decimals with up to three |
| lengths | Record lengths and distances using <br> decimal places | kilometres, metres, <br> the abbreviations $\mathrm{km}, \mathrm{m}, \mathrm{cm}$ and mm | Convert between millilitres and <br> litres |  |

## Content Cluster 4: Comparing quantities - area/volume/mass focus (numbers can be compared based on size and place value)

## Fractions and Decimals 1

## MA3-7NA

Compare and order unit fractions with denominators

2, 3, 4, 5, 6, 8, 10, 12
and 100
Compare, order and represent decimals with up to three decimal places

Area 1 MA3-10MG
Recognise the need for square kilometres and hectares to measure area Record areas using the abbreviations $\mathrm{km}_{2}$ and ha

## Volume and Capacity 1 MA3-

 11MGUse cubic centimetres and cubic metres to measure and estimate volumes

Select and use appropriate units to measure volume

Record volumes using the abbreviations $\mathrm{cm}_{3}$ and $\mathrm{m}_{3}$

## Mass 1 MA3-12MG

Recognise the need for tonnes to measure mass
Record masses using the abbreviations $\mathrm{t}, \mathrm{kg}$ and g
Select and use appropriate instruments and units to measure mass
Solve problems involving mass
Mass 2 MA3-12MG
Record mass using decimal notation to three decimal places
Convert between tonnes, kilograms and grams

## Stage 3 Content Clusters

| Content Cluster 5: Partitioning: Part-whole number knowledge (numbers can be partitioned in multiple ways) |  |  |  |
| :---: | :---: | :---: | :---: |
| Whole Numbers 1 MA3-4NA <br> Record numbers of any size using expanded notation <br> Whole Numbers 2 MA3-4NA <br> Identify and describe prime and composite numbers | Fractions and Decimals 1 MA3-7NA <br> Compare and order unit fractions with denominators $2,3,4,5,6,8,10,12$ and 100 <br> Express mixed numerals as improper fractions and vice versa | Fractions and Decimals 2 MA3-7NA <br> Represent, compare and order fractions with denominators $2,3,4,5,6,8,10,12$ and 100 Write fractions in their 'simplest form' | Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to divide numbers with three or more digits by a one-digit operator, including problems that result in a remainder |


| Content Cluster 6: Flexible strategies for operating with numbers (numbers can be partitioned to assist with computation) |  |  |
| :---: | :---: | :---: |
| Addition and Subtraction 1 MA3-5NA <br> Select and apply efficient mental, written and calculator strategies for addition and subtraction of numbers of any size | Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators Use and record a range of mental and written strategies to divide numbers with three or more digits by a one-digit operator, including problems that result in a remainder | Fractions and Decimals 1 MA3-7NA <br> Model and represent strategies to add and subtract fractions with the same denominator <br> Fractions and Decimals 2 MA3-7NA <br> Add and subtract fractions, included mixed numerals, with the same or related denominators <br> Use mental, written and calculator strategies to add and subtract decimals with up to three decimal places <br> Use mental, written and calculator strategies to multiply decimals by one- and two-digit whole numbers <br> Use mental, written and calculator strategies to divide decimals by one-digit whole numbers |

## Primary

 Learning
## Stage 3 Content Clusters

| Content Cluster 7: A variety of strategies can be applied to solve word problems |  |  |  |
| :--- | :--- | :--- | :--- |
| Addition and Subtraction 1 | Addition and Subtraction 2 MA3-5NA | Multiplication and Division 1 MA3-6NA | Fractions and Decimals 2 |
| MA3-5NA | Select and apply efficient mental, written and | Solve word problems and record the | MA3-7NA |
| Solve word problems and | calculator strategies to solve word problems | strategy used | Solve word problems involving |
| record the strategy used, | and record the strategy used | Multiplication and Division 2 MA3-6NA | fractions and decimals, |
| including problems involving |  | Select and apply efficient mental, written and <br> money |  |
| including money problems |  |  |  |
| record the strategy used |  |  |  |

## Content Cluster 8: Multiples can be visually represented as an array ('for each' number structure)

| Multiplication and Division 1 MA3-6NA | Multiplication and Division 2 MA3-6NA | Area 1 MA3-10MG | Volume and | Patterns and Algebra 2 |
| :---: | :---: | :---: | :---: | :---: |
| Use and record a range of mental and | Select and apply efficient mental, | Develop a strategy to find | Capacity 2 MA3- | MA3-8NA |
| written strategies to multiply by one- and | written and calculator strategies to | areas of rectangles (including | 11MG | Continue, create, record |
| two-digit operators | solve word problems and record the | squares) and record the | Develop a strategy | and describe geometric |
| Use and record a range of mental and | strategy used | strategy in words | to find volumes of | and number patterns in |
| written strategies to divide numbers with |  | Area 2 MA3-10MG | rectangular prisms | words |
| three or more digits by a one-digit |  | Develop a strategy to find | and record the |  |
| operator, including problems that result in a remainder |  | areas of triangles and record the strategy in words | strategy in words |  |

## Stage 3 Content Clusters

| Content Cluster 9: Reasonableness of solutions can be checked using estimation |  |  |  |
| :---: | :---: | :---: | :---: |
| Addition and Subtraction 1 MA3-5NA <br> Use estimation to check answers to calculations Solve word problems and record the strategy used, including problems involving money | Multiplication and Division 1 MA3-6NA <br> Solve word problems and record the strategy used <br> Use estimation to check answers to calculations | Multiplication and Division 2 MA3-6NA <br> Select and apply efficient mental, written and calculator strategies to solve word problems and record the strategy used | Fractions and Decimals 2 MA3-7NA <br> Solve word problems involving fractions and decimals, including money problems |

Content Cluster 10: Benchmark numbers can be used to estimate quantities (how much/how many)

| Addition and Subtraction 1 MA3-5NA <br> Use estimation to check answers to calculations | Multiplication and <br> Division 1 MA3-6NA <br> Solve word problems and record the strategy used Use estimation to check answers to calculations | Fractions and Decimals <br> 2 MA3-7NA <br> Make connections between equivalent percentages, fractions and decimals | Volume and Capacity 1 MA3-11MG <br> Use cubic centimetres and cubic metres to measure and estimate volumes <br> Select and use appropriate units to measure volume | Angles 1 MA3-16MG <br> Measure, compare and estimate angles in degrees (up to $360^{\circ}$ ) <br> Record angle measurements using the symbol for degrees $\left({ }^{\circ}\right)$ |
| :---: | :---: | :---: | :---: | :---: |

## Stage 3 Content Clusters

| Content Cluster 11: Number relationships - converting (e.g. one thousand can be regrouped as 10 hundreds, 100 tens, or 1000 ones) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Whole Numbers 1 MA3-4NA <br> Read, write and order numbers of any size <br> State the place value of digits in numbers of any size <br> Record numbers of any size using expanded notation | Time 1MA3-13MG <br> Convert between 12and 24-hour time Determine and compare the duration of events | Fractions and Decimals 1 MA3-7NA <br> Apply the place value system to represent thousandths as decimals <br> Fractions and Decimals 2 MA3-7NA <br> Multiply and divide decimals by 10, 100 and 1000 | Length 2 MA3-9MG <br> Convert between kilometres, metres, centimetres and millimetres | Volume and Capacity 2 <br> MA3-11MG <br> Convert between millilitres and litres | Mass 2 MA3-12MG <br> Convert between tonnes, kilograms and grams |

## Content Cluster 12: Money uses a many-to-one scale (link to place value e.g. 100 cents is equal to \$1)

| Addition and Subtraction 1 MA3-5NA | Multiplication and Division 1 MA3-6NA | Fractions and Decimals 2 MA3-7NA |
| :--- | :--- | :--- |
| Solve word problems and record the strategy used, | Solve word problems and record the | Solve word problems involving fractions and decimals, including money |
| including problems involving money | strategy used <br> Create a simple budget | Interpret remainders in division problems <br> Use mental, written and calculator strategies to calculate 10\%, 25\% |
| and 50\% of quantities, including as discounts |  |  |


| Content Cluster 13: The 'equals sign' means "the same as" (equality and inequality) |  |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: |
| Multiplication and Division 2 MA3-6NA | Patterns and Algebra 1 MA3-8NA | Fractions and Decimals 2 MA3-7NA |  |  |  |  |
| Recognise and use grouping symbols | Find missing numbers in number sentences involving <br> multiplication or division on one or both sides of the equals <br> sign | Determine, generate and record equivalent fractions <br> Make connections between equivalent percentages, fractions <br> and decimals |  |  |  |  |

## Primary

Learning

## Stage 3 Content Clusters

Content Cluster 14: Numbers can be represented using pairs to explore odd and even properties

Patterns and Algebra 1 MA3-8NA
Identify, continue create and describe increasing and decreasing number patterns with fractions, decimals and whole numbers

Whole Numbers 1 MA3-4NA<br>Determine factors and multiples of whole numbers<br>Whole Numbers 2 MA3-4NA<br>Identify and describe prime and composite numbers<br>Model and describe square and triangular numbers

| Content Cluster 15: Patterns repeat or grow and future terms can be predicted (number structure) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Patterns and Algebra 1 MA38NA <br> Identify, continue create and describe increasing and decreasing number patterns with fractions, decimals and whole numbers | Multiplication and Division 1 MA3-6NA <br> Use and record a range of mental and written strategies to multiply by one- and two-digit operators | Fractions and Decimals 1 MA3-7NA <br> Model and represent strategies to add and subtract fractions with the same denominator Fractions and Decimals 2 MA3-7NA <br> Use mental, written and calculator strategies to add and subtract decimals with up to three decimal places <br> Use mental, written and calculator strategies to multiply decimals by one- and two-digit whole numbers <br> Use mental, written and calculator strategies to divide decimals by one-digit whole numbers | Whole Numbers 1 MA3-4NA <br> Read, write and order numbers of any size Whole Numbers 2 MA3-4NA <br> Model and describe square and triangular numbers | Addition and Subtraction 1 MA35NA <br> Select and apply efficient mental, written and calculator strategies for addition and subtraction of numbers of any size |

## Stage 3 Content Clusters

| Content Cluster 16: Patterns can be represented geometrically |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Patterns and Algebra 2 MA3-8NA <br> Continue, create, record and describe geometric and number patterns in words <br> Determine the rule for geometric and number patterns in words and use the rule to calculate values | Multiplication and Division 1 MA3-6NA Use and record a range of mental and written strategies to multiply by one- and two-digit operators | Two-Dimensional Space 1 MA3-15MG <br> Classify and draw regular and irregular two-dimensional shapes from descriptions of their features Use the terms 'translate', 'reflect' and 'rotate' to describe transformations of shapes Two-Dimensional Space 2 MA3-15MG Identify, use and describe combinations of translations, reflections and rotations | Whole Numbers 1 MA3-4NA <br> Read, write and order numbers of any size <br> Whole Numbers 2 MA3-4NA <br> Model and describe square and triangular numbers | Addition and Subtraction 1 MA35NA <br> Select and apply efficient mental, written and calculator strategies for addition and subtraction of numbers of any size |

## Content Cluster 17: A fraction is a number (that represents a relationship between parts and the whole)

| Fractions and Decimals 1 MA3-7NA | Fractions and Decimals 2 MA3-7NA |
| :--- | :--- |
| Compare and order unit fractions with | Represent, compare and order fractions with denominators |
| denominators 2, 3, 4, 5, 6, 8, 10, 12 and 100 | $2,3,4,5,6,8,10,12$ and 100 |
| Express mixed numerals as improper fractions | Determine, generate and record equivalent fractions |
| and vice versa | Write fractions in their 'simplest form' |
|  | Make connections between equivalent percentages, fractions and |
|  | decimals |

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## Stage 3 Content Clusters

## Content Cluster 18: Fractions represent division (number relationships)

| Fractions and Decimals 1 MA3- | Fractions and Decimals 2 MA3-7NA | Multiplication and Division 1 MA3-6NA | Patterns and Algebra 1 MA3-8NA |
| :--- | :--- | :--- | :--- |
| 7NA | Represent, compare and order fractions | Use and record a range of mental and | Identify, continue create and describe |
| Compare and order unit fractions | with denominators 2, 3, 4,5,6,8,10,12 | written strategies to divide numbers with | increasing and decreasing number patterns |
| with denominators | and 100 | three or more digits by a one-digit operator, | with fractions, decimals and whole numbers |
| $2,3,4,5,6,8,10,12$ and 100 | Determine, generate and record | including problems that result in a remainder |  |
| Express mixed numerals as | equivalent fractions | Interpret remainders in division problems |  |
| improper fractions and vice versa | Write fractions in their 'simplest form' |  |  |


| Content Cluster 19: Fractions as a measure |  |  |  |
| :---: | :---: | :---: | :---: |
| Fractions and Decimals 1 MA37NA <br> Model and represent strategies to add and subtract fractions with the same denominator <br> Fractions and Decimals 2 MA37NA <br> Add and subtract fractions, included mixed numerals, with the same or related denominators | Length 1 MA3-9MG <br> Record lengths and distances using the abbreviations $\mathrm{km}, \mathrm{m}, \mathrm{cm}$ and mm Find perimeters of common twodimensional shapes and record the strategy <br> Length 2 MA3-9MG <br> Convert between kilometres, metres, centimetres and millimetres Solve problems involving length and perimeter | Area 1 MA3-10MG <br> Recognise the need for square kilometres and hectares to measure area <br> Record areas using the abbreviations $\mathrm{km}_{2}$ and ha <br> Develop a strategy to find areas of rectangles (including squares) and record the strategy in words <br> Area 2 MA3-10MG <br> Develop a strategy to find areas of triangles and record the strategy in words <br> Solve problems involving areas of rectangles (including squares) and triangles | Time 1MA3-13MG <br> Convert between 12- and 24-hour time <br> Time 2 MA3-13MG <br> Interpret and use timetables |

## Primary

## Stage 3 Content Clusters

| Content Cluster 20: Fractions as an operator |  |  |  |
| :---: | :---: | :---: | :---: |
| Fractions and Decimals 2 MA3-7NA <br> Multiply fractions by whole numbers <br> Find a simple fraction of a quantity <br> Solve word problems involving fractions and decimals, including money problems <br> Make connections between equivalent percentages, fractions and decimals <br> Use mental, written and calculator strategies to calculate $10 \%, 25 \%$ and $50 \%$ of quantities, including as discounts | Addition and Subtraction 1 MA35NA <br> Solve word problems and record the strategy used, including problems involving money <br> Create a simple budget | Multiplication and Division 1 MA3-6NA <br> Use and record a range of mental and written strategies to multiply by one- and two-digit operators | Area 2 MA3-10MG <br> Solve problems involving areas of rectangles (including squares) and triangles |

## Content Cluster 21: Time can be measured and compared in hours, minutes and seconds (relating 12 to 24 hour time)

| Time 1MA3-13MG | Time 2 MA3-13MG | Fractions and Decimals 1 MA3-7NA |  |
| :--- | :--- | :--- | :--- |
| Convert between 12- and 24-hour time | Interpret and use timetables | Addition and Subtraction 2 MA3-5NA <br> Model and represent strategies to <br> add and subtract fractions with the <br> of events and apply efficient mental, written and <br> same denominator | calculator strategies to solve word problems and <br> record the strategy used |

## Primary

 Learning
## Stage 3 Content Clusters

| Multiplication and | Length 1 MA3-9MG | Position MA3-17MG | Data 1 MA3-18SP | Time 2 MA3- | Two-Dimensional |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Division 1 MA3-6NA | Select and use appropriate | Use grid-referenced maps to | Construct data displays, | 13MG | Space 1 MA3- |
| Use and record a | instruments and units to measure | locate and describe positions | including tables, column graphs, | Draw and | 15MG |
| range of mental and | lengths | Follow a sequence of directions, | dot plots and line graphs, | interpret | Make and compare |
| written strategies to | Record lengths and distances using | including compass directions, to | appropriate for the data type | timelines using a given scale | enlargements of shapes/pictures |
| two-digit operators | the abbreviations $\mathrm{km}, \mathrm{m}, \mathrm{cm}$ and mm Length 2 MA3-9MG | find a particular location on a map <br> Describe routes using landmarks | Describe and interpret data presented in tables, column | a given scale | shapes/pictures |
|  | Convert between kilometres, metres, centimetres and millimetres | and directional language | graphs, dot plots and line graphs |  |  |


| Content Cluster 23: Measurements are approximations and can be represented using formal units |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Length 1 MA3-9MG <br> Record lengths and distances using the abbreviations km, m, cm and mm <br> Length 2 MA3-9MG <br> Record lengths and distances using decimal notation to three decimal places | Area 1 MA3-10MG <br> Record areas using the abbreviations km 2 and ha | Volume and Capacity 1 MA311MG <br> Record volumes using the abbreviations $\mathrm{cm}_{3}$ and $\mathrm{m}_{3}$ Volume and Capacity 2 MA211MG <br> Record volumes and capacities using decimal notation to three decimal places <br> Convert between millilitres and litres | Mass 1 MA3-12MG <br> Recognise the need for tonnes to measure mass <br> Record masses using the abbreviations t , kg and g <br> Distinguish between 'gross mass' and 'net mass' <br> Mass 2 MA3-12MG <br> Record mass using decimal notation to three decimal places | Angles 1 MA3-16MG <br> Recognise the need for formal units to measure angles <br> Record angle measurements using the symbol for degrees ( ${ }^{\circ}$ ) <br> Construct angles using a protractor (up to $360^{\circ}$ ) <br> Describe angle size in degrees for each angle classification |

## Primary

## Stage 3 Content Clusters

Content Cluster 24: The multiplicative structure (row and column) can be applied to measure area and volume

| Multiplication and | Fraction and Decimals 2 | Area 1 MA3-10MG | Volume and Capacity 2 MA3- | Three-Dimensional Space 2 MA3- |
| :---: | :---: | :---: | :---: | :---: |
| Division 1 MA3-6NA | MA3-7NA | Develop a strategy to find areas of | 11MG | 14MG |
| Use and record a range | Use mental, written and | rectangles (including squares) and | Develop a strategy to find | Construct prisms and pyramids |
| of mental and written | calculator strategies | record the strategy in words | volumes of rectangular prisms | using a variety of materials, and |
| strategies to multiply by | to multiply decimals by one- | Area 2 MA3-10MG | and record the strategy | given drawings from different |
| one- and two-digit operators | and two-digit whole numbers | Develop a strategy to find areas of triangles and record the strategy in words | in words | views |

## Content Cluster 25: Objects can be measured and compared through different representations

| Three-dimensional Space 1 MA3-14MG | Volume and Capacity 1 MA3-11MG |
| :--- | :--- |
| Describe and compare properties of prisms and | Use cubic centimetres and cubic metres to measure and |
| pyramids in terms of their faces, edges and vertices | estimate volumes |
| Connect three-dimensional objects with their nets | Select and use appropriate units to measure volume |
| Three-Dimensional Space 2 MA3-14MG | Volume and Capacity 2 MA3-11MG |
| Construct prisms and pyramids using a variety of | Connect volume and capacity and their units |
| materials, and given drawings from different views | of measurement <br> Develop a strategy to find volumes of rectangular prisms <br> and record the strategy in words |
|  |  |

## Multiplication and Division 1 MA3-6NA

Use and record a range of mental and written strategies to multiply by one- and two-digit operators

## Primary

## Stage 3 Content Clusters

| Content Cluster 26: Shapes can be measured and compared through different representations |  |  |  |
| :---: | :---: | :---: | :---: |
| Two-Dimensional Space 1 MA3-15MG Identify, name and draw right-angled, equilateral, isosceles and scalene triangles <br> Compare and describe side properties of the special quadrilaterals and special triangles <br> Explore angle properties of the special quadrilaterals and special triangles | Area 1 MA3-10MG <br> Develop a strategy to find areas of rectangles (including squares) and record the strategy in words <br> Area 2 MA3-10MG <br> Develop a strategy to find areas of triangles and record the strategy in words | Length 1 MA3-9MG <br> Find perimeters of common twodimensional shapes and record the strategy | Angles 1 MA3-16MG <br> Measure, compare and estimate angles in degrees (up to $360^{\circ}$ ) <br> Describe angle size in degrees for each angle classification |

## Content Cluster 27: Shape and objects are classified based on their properties

## Three-Dimensional Space 1 MA3-

 14MGName prisms and pyramids according to the shape of their 'base' Recognise that prisms have a uniform cross-section and pyramids do not
Describe and compare properties of prisms and pyramids in terms of their faces, edges and vertices

## Two-Dimensional Space 1 MA3-15MG

Identify, name and draw right-angled, equilateral, isosceles and scalene triangles

Compare and describe side properties of the special quadrilaterals and special triangles

Explore angle properties of the special quadrilaterals and special triangles
Classify and draw regular and irregular two-dimensional
shapes from descriptions of their features
Identify line and rotational symmetries

## Two-Dimensional Space 2 MA3-

 15MGIdentify, describe, compare and draw diagonals of two-dimensional shapes

Identify and name parts of circles

## Angles 2 MA3-16MG

Identify and name angle types formed by the intersection of straight lines, including 'angles on a straight line', 'angles at a point' and 'vertically opposite angles
Use known angle results to find unknown angles in diagrams

## Stage 3 Content Clusters

| Content Cluster 28: Grid references and coordinates can be used for locating and positioning |  |  |  |
| :---: | :---: | :---: | :---: |
| Position 1 MA3-17MG <br> Use grid-referenced maps to locate and describe positions | Patterns and Algebra 2 MA38NA <br> Locate and record the coordinates of points in all four quadrants of the Cartesian plane | Two-Dimensional Space 1 MA3-15MG <br> Use the terms 'translate', 'reflect' and 'rotate' to describe transformations of shapes <br> Make and compare enlargements of shapes/pictures <br> Two-Dimensional Space 2 MA3-15MG <br> Identify, use and describe combinations of translations, reflections and rotations | Three-Dimensional Space 2 MA314MG <br> Construct prisms and pyramids using a variety of materials, and given drawings from different views |


| Data 1 MA3-18SP <br> Collect categorical and numerical data by observation and by survey Describe and interpret data presented in tables, column graphs, dot plots and line graphs | Data 2 MA3-18SP | Chance 1 MA3-19SP | Addition and Subtraction | Multiplication and Division |
| :---: | :---: | :---: | :---: | :---: |
|  | Interpret and create two-way | List outcomes of chance experiments | 1 MA3-5NA | 1 MA3-6NA |
|  | tables | involving equally likely outcomes | Select and apply efficient | Use and record a range |
|  | Interpret side-by-side column | Chance 2 MA3-19SP | mental, written | of mental and written |
|  | graphs | Conduct chance experiments with | and calculator strategies | strategies to divide |
|  | Compare a range of data displays to determine the most appropriate display for particular sets of data | both small and large numbers of trials | for addition and subtraction of numbers of any size | numbers with three or more digits by a one-digit operator |
|  | Interpret and critically evaluate data presented in digital media and elsewhere |  |  |  |

## Stage 3 Content Clusters

| Content Cluster 30: Information can be presented visually to convey meaning (data representations and exploring bias) |  |  |  |
| :--- | :--- | :--- | :--- |
| Data 1 MA3-18SP | Data 2 MA3-18SP | Angles 1 MA3-16MG |  |
| Construct data displays, including tables, | Interpret and create two-way tables <br> column graphs, dot plots and line <br> graphs, appropriate for the data type <br> Compare a range of data displays to <br> determine the most appropriate display <br> for particular sets of data | (up to 360 $)$ | Length 1 MA3-9MG |
| Select and use appropriate |  |  |  |
| instruments and units to measure |  |  |  |
| lengths |  |  |  |

## Content Cluster 31: Events can be predicted, compared, and analysed based on probability

Chance 1 MA3-19SP
List outcomes of chance experiments
involving equally likely outcomes

Chance 2 MA3-19SP
Compare observed frequencies in chance experiments with expected frequencies Conduct chance experiments with both small
and large numbers of trials

Data 1 MA3-18SP
Collect categorical and numerical data by observation and by survey
Describe and interpret data presented in tables, column graphs, dot plots and line graphs

Content Cluster 32: Probabilities of events can be described in a range of 0-1 (probabilities as fractions of a whole)

| Chance 1 MA3-19SP | Chance 2 MA3-19SP | Data 1 MA3-18SP | Fractions and Decimals 2 MA3-7NA |
| :--- | :--- | :--- | :--- |
| Represent probabilities using fractions | Compare observed frequencies in chance | Collect categorical and numerical |  |
| Recognise that probabilities range from |  |  |  |
| 0 to 1 | experiments with expected frequencies <br> Represent probabilities using fractions, compare and order fractions with <br> decimals and percentages | data by observation and by survey | denominators 2,3,4,5,6,8,10,12 and 100 |
| Solve word problems involving fractions and |  |  |  |
| decimals |  |  |  |


[^0]:    Whole Numbers 2 MA3-4NA
    Read, write and order numbers of any
    size
    State the place value of digits in numbers of any size
    Record numbers of any size using expanded notation

